A-DSP: An Adaptive Join Algorithm for Dynamic Data Stream on Cloud System

Junhua Fang, Rong Zhang©, Yan Zhao©, Kai Zheng©, Member, IEEE, Xiaofang Zhou©, Fellow, IEEE, and Aoying Zhou

Abstract—The join operations, including both equi and non-equi joins, are essential to the complex data analytics in the big data era. However, they are not inherently supported by existing DSPEs (Distributed Stream Processing Engines). The state-of-the-art join solutions on DSPEs rely on either complicated routing strategies or resource-inefficient processing structures, which are susceptible to dynamic workload, especially when the DSPEs face various join predicate operations and skewed data distribution. In this paper, we propose a new cost-effective stream join framework, named A-DSP (Adaptive Dimensional Space Processing), which enhances the adaptability of real-time join model and minimizes the resource used over the dynamic workloads. Our proposal includes: 1) a join model generation algorithm devised to adaptively switch between different join schemes so as to minimize the number of processing task required; 2) a load-balancing mechanism which maximizes the processing throughput; and 3) a lightweight algorithm designed for cutting down unnecessary migration cost. Extensive experiments are conducted to compare our proposal against state-of-the-art solutions on both benchmark and real-world workloads. The experimental results verify the effectiveness of our method, especially on reducing the operational cost under pay-as-you-go pricing scheme.

Index Terms—Distributed stream join, theta-join, cost effective

1 INTRODUCTION

The big data era has urged the techniques for real-time data processing in various domains, such as stock trading analysis, traffic monitoring and network measurement. Introduction of distributed and parallel processing frameworks enables the efficient processing of massive streams. However, the load balancing issue [1], [2], [3], [4], [5] is emerging as a common problem to those parallel processing frameworks, which deteriorates the performance of the distributed platform on big data processing. Extensive efforts are devoted to tackle the load balancing issue for different operators, including summarization [6], aggregation [7], join [3], [8], [9], [10], etc. Among these operations, $\theta$-join [11], [12], [13] is recognized as the most challenging one, due to its large variety in join predicate options $\{>, \geq, <, \leq, =, \neq\}$.

In practice, $\theta$-join should be supported as a basic operation. For instance, band-joins are common in spatial applications [14], and similarity joins between data sets are also necessary in correlation analysis [13]. There are a handful of approaches designed for join operator over fast and continuous streams, which falls into two categories: 1-DSP (1-dimensional space processing) model [7], [15], [16], [17], [18] and 2-DSP (2-dimensional space processing) model [10], [11], [12], [13]. We use $m$ to denote the task instance in DSPE. For 1-DSP, we map the key space $K$ in any stream to $m$ tasks by a dividing function $F$ (e.g., range function, consistent hashing, etc.), which is defined as $F(k_i) \rightarrow m_a$, with $k_i \in K$ and $0 \leq m_a \leq m - 1$. As shown in Fig. 1a, it has three tasks numbered by $m_{0-2}$. Any key from either stream $R$ or $S$ is supposed to be assigned to one of the tasks. On the other hand, 2-DSP arranges tasks into two dimensional space, where each dimension represents the division of one stream. As in Fig. 1b, it organizes the tasks as a matrix, represented as $m_{ij}$, with $0 \leq i \leq 1$ and $0 \leq j \leq 1$. And stream $S$ and $R$ are divided along the horizontal and vertical dimension respectively. More specifically, the processing mode of these two models are explained as follows:

1-DSP. In Fig. 1a, stream $R$ ($S$) is split into three sub-streams $r_i$ ($s_i$) for join processing and stored locally in $m_i$, with $0 \leq i \leq 2$. However, for non-equi join, a join tuple may get involved in multiple local join tasks according to join predicates ($\theta$). In addition to the locally stored sub-stream $r_i$ in task $m_i$, additional sub-stream $r'_i$ is sent to $m_i$ for join purpose with locally stored tuples $s_i$, which contain tuples to be joined but not included in $r_i$. Therefore, 1-DSP has two routing methods, one for local storage (Storage routing, i.e., $R_i$) and the other one for join routing (Join routing, i.e., $R'_i$) defined by the join predicate as shown in Fig. 1a. During the

---

*J. Fang and Y. Zhao are with the Institute of Artificial Intelligence, School of Computer Science and Technology, Soochow University, Suzhou, Jiangsu, China. E-mail: j.fang@soc.suda.edu.cn.
R. Zhang and A. Zhou are with the School of Data Science and Engineering, East China Normal University, Shanghai 3663, China. E-mail: rzhang@sei.ecnu.edu.cn, azhou@dase.ecnu.edu.cn.
K. Zheng is with the University of Electronic Science and Technology of China, Chengdu, Sichuan 610054, China. E-mail: zhengkai@uestc.edu.cn.
X. Zhou is with the School of Information Technology and Electrical Engineering, The University of Queensland, Brisbane, QLD 4072, Australia. E-mail: xzf@itee.uq.edu.au.

Digital Object Identifier no. 10.1109/TKDE.2019.2947055
join process, the destination of the incoming tuple, e.g., $r_i$, is determined by two different routing strategies: storage routing $R_t$ decides its storage task, while join routing $R_J$ determines to which task(s) $r_i$ shall be assigned to produce join results. In other words, the $R_J(S_J)$ acts only when $R_t(S_t)$ can not make the complete results for any join predicate; otherwise, join routing is useless where $R_J = \emptyset (S_J = \emptyset)$.

2-DSP. Join-matrix model is a typical represent for 2-DSP, in which a partitioning scheme is employed on each dimension to split the incoming stream data randomly into a set of mutually exclusive sub-streams to promise the balance requirement. As shown in Fig. 1b, stream $R$ is randomly split into two sub-streams $r_0$ and $r_1$ along the vertical side, with $r_0 \cap r_1 = \emptyset$ ($s_0$ and $s_1$ for $S$ respectively). Therefore, $R \bowtie S$ is decomposed into four sub-tasks, each of which $m_{ij}$ ($0 \leq i, j \leq 1$) takes a pair of sub-streams from $R$ and $S$. The join-matrix model can always return complete results for any join predicate as it can promise each pair of tuples from two data streams meet once.

In fact, different processing models have their respective performance characteristics. Table 1 exhibits the advantages and disadvantages of 1-DSP and 2-DSP from perspectives of resource consumption, application scope, and operational status. In accordance to the routing strategies in Fig. 1, it is not difficult to find that 1-DSP is a content-sensitive partitioning scheme, while 2-DSP uses the random partition strategy determining it is a content-insensitive one. This also explains the fundamental differences exhibited in Table 1. Specifically, 1-DSP is a resource-saving join model because it is unnecessary to maintain a specific processing architecture. Instead, it consumes resources on demand. However, having a content-sensitive distribution strategy decides that 1-DSP is only better for the small-scale join (e.g., equal-join) and clumsy in a dynamic distribution and skewed environment. For 2-DSP, although its content-insensitive partition strategy enables it to support the arbitrary join predicate and handle data skewness perfectly, this is at the high cost of task consumption because this model must maintain a specific processing architecture.

In this paper, we propose a flexible and adaptive model, named A-DSP (Adaptive Dimensional Space Processing), for parallel stream join. By integrating the processing strategies of 1-DSP and 2-DSP. In other words, we break the limit of processing scheme in 1-DSP and 2-DSP with a new solution for parallel $\theta$-join to explore a much larger optimization space: maximizing the resource utilization, supporting various join predicates and guaranteeing workload balance among parallel tasks. In contrast to up-to-date studies, A-DSP has several advantages as follows. First, this scheme achieves high flexibility by easily redirecting the keys to new worker threads with simple editing on the routing function. Second, it is highly efficient when the system faces $\theta$-join and dynamic incoming workload, by providing a general strategy to generate the partition function for data balance under dynamic stream. Moreover, workload redistribution with the scheme is scalable and effective, by allowing the system to respond promptly to the short-term workload fluctuation even when there are heavy traffic of tuples present in the incoming data stream.

Although our preliminary work in [19] has already optimized the join performance by designing a varietal matrix join model based on 2-DSP, it is still fails to get rid of the inherent and insurmountable disadvantages of regular matrix model. To fully unleash the power of our A-DSP model for minimizing the operational cost while maximizing the processing throughput over various join predicate requirement, a suite of optimization techniques are introduced for our syncretic processing scheme to fully exploit the benefits of 1-DSP and 2-DSP. In summary, the major contributions of this work are summarized as:

- We propose the A-DSP join model to reduce the operational cost with full support of arbitrary join predicates while guaranteeing the correctness of join results.
- We devise the scheme generation algorithms for our A-DSP model. Moreover, we present a detailed theoretical analysis for proposed algorithms, and prove their usability and correctness.
- We design a lightweight computation model to support rapid migration plan generation, which incurs minimal data transmission overhead and processing latency.
- We empirically evaluate our model against the state-of-the-art solutions on both standard benchmarks and real-world stream data workloads with detailed explanations on experimental results.

The remainder of this paper is organized as follows. Section 2 introduces the preliminaries. Section 3 describes how to generate the processing scheme. Section 4 explains the detailed implementation of our proposed method. Section 5 shows the experimental results. Section 6 reviews the existing studies on stream join processing in distributed systems. Section 7 finally concludes the paper and discusses future research directions.

### 2 Preliminaries

#### 2.1 Definitions

Join matrix model organizes the parallel processing tasks as a matrix to handle the join operation between two incoming streams, where each side of which corresponds to one

---

**TABLE 1** Summary of the Advantages and Disadvantages of Different Models

<table>
<thead>
<tr>
<th>Model</th>
<th>Resource saving</th>
<th>Arbitrary join</th>
<th>Workload balance</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-DSP</td>
<td>✓</td>
<td>×</td>
<td>×</td>
</tr>
<tr>
<td>2-DSP</td>
<td>×</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>A-DSP (Our)</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
</tbody>
</table>

---

Fig. 1. Two typical paradigms of existing stream join models.
Table 2
Table of Notations

<table>
<thead>
<tr>
<th>Notations</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>R, S</td>
<td>R, S stream</td>
</tr>
<tr>
<td>C / C̄</td>
<td>tuple matrix without/with ordered join key</td>
</tr>
<tr>
<td>CA / CĀ</td>
<td>complete information area of C / C̄</td>
</tr>
<tr>
<td>ca / c̄a</td>
<td>coverage area without/with ordered join key</td>
</tr>
<tr>
<td>TaskA</td>
<td>the area that is feasible to a single task</td>
</tr>
<tr>
<td>c(i,j)</td>
<td>the cell located in the i-th row and j-th column</td>
</tr>
<tr>
<td>[c(i,j),c(i',j')]</td>
<td>the rectangle from c(i,j) to c(i',j')</td>
</tr>
<tr>
<td>c̄a</td>
<td>the x-th c̄a</td>
</tr>
<tr>
<td>TaskAji(TaskAij)</td>
<td>the TaskA in the i-th row, j-th column of ca(cai,caj)</td>
</tr>
<tr>
<td>a/b(a'/b')</td>
<td>the TaskA number of rows/columns in ca(cai,caj)</td>
</tr>
<tr>
<td>c̄a/c̄a</td>
<td>the tuple set of rows/columns/output set in area c̄a</td>
</tr>
<tr>
<td>V((\bar{V}))</td>
<td>memory size of task (half size (\bar{V}))</td>
</tr>
</tbody>
</table>

Since the stream is dynamic, we define the universal set of tuples arranged by join matrix model as tuple matrix, denoted by C. The tuple matrix enumerates all tuple pairs of the different streams, that is, assigning the Cartesian product of R and S (R X S) as a tuple matrix. We use cell c(i,j) to denote the tuple pair of the i-th row and j-th column of tuple matrix. Table 2 lists the notations commonly used in the rest of the paper.

Definition 1. Given the streams R and S, if their tuple matrix orders its two side tuples both by their join key, then the matrix is defined as Ordered tuple matrix, denoted by C̄.

Definition 2. In tuple matrix C / C̄, we refer to the set of cells that covered by a rectangle as Coverage area, denoted by ca/cā. The rectangle is represented by \([c(i,j),c(i',j')]\), meaning its upper left corner is c(i,j) and lower right is c(i',j').

Definition 3. In C̄, we define the set of cells comprised by a series of 1) non-overlapping, 2) non-overlapping, and 3) results completion c̄as as Complete information area, denoted by CA. The constraints of c̄as are defined as:

(1) No-interval. This property requires that the complete set of c̄as is able to cover all incoming tuples in both the horizontal and vertical directions, which can be expressed as \(\bigcup_{c_i\in C} \neg c̄a = R\) and \(\bigcup_{c_j\in C} \neg c̄a = S\).

(2) Non-overlapping. This property requires that each cell in CA should be covered by the complete set of c̄as at most once, which can be expressed as \(\forall_{c_i\in C}, c̄a_j\in CA, i\neq j\), then \(c̄a_i\cap c̄a_j = \emptyset\).

(3) Results completion. This property requires that all join results in C̄ should be covered by CA, which can be expressed as \(\bigcup_{c_i\in C} \neg c̄a = C̄\).

Definition 4. In tuple matrix, we call the coverage area that assigned to single one task instance as Task area, denoted by TaskA.

Fig. 2 shows a toy example of join operation using tuple matrix. Each stream (R / S) has 12 tuples and their join key is denoted by R / S / K. Its join condition is \(|R.K - S.K|\leq 2\), and cells which produce join results are marked in grey. Then, the tuple matrix in Fig. 2a can be seen as a C according to Definition 1, and in Fig. 2c, the union of c01 and c02 can be regarded as a CA according to Def3. Furthermore, based on Definition 3, C will be treated as a complete information area, since its out-of-order tuples make each cell in C become a potential result (CA = C̄), which can be reflected by Fig. 2b.

2.2 Models

Based on the above definitions, the essence of parallel processing of those different methods is partitioning the whole tuple matrix into multi-TaskA s. As shown in Table 3, 1-DSP and 2-DSP can be expressed as splitting CA and CA into multi-TaskA s, respectively. Figs. 2a and 2b show their data partition results. They also reflect the characteristics of the two methods shown in Table 1, that is, 1-DSP uses less resources, but exists workload imbalance, while 2-DSP is the opposite. Specifically, the workload of each task instance includes input workload and output workload, which can be measured by the number of tuples flowing in and out [10]. For example in Fig. 3, we assume the maximum input workload is 8 and the maximum output workload is 5. Then, 4 tasks in Fig. 2a set an imbalance status while 9 tasks in Fig. 2b provide a perfect balance both in input and output workload. In fact, only the balance of input workload needs to be taken into account while using 2-DSP, for its tuple-based random routing strategy can ensure the output results being evenly distributed in tasks. Our subsequent approach inherits this advantage.

The partitioning process of A-DSP model mainly consists of two phases: partition CA into c̄as and partition c̄a into TaskA s, denoted by P~ and Pca, respectively. For each c̄a generated by Pca, P~ takes it as an unordered c̄a, and then, partitions it into multi-TaskA s using 2-DSP. Intuitively, using 1-DSP to generate c̄as in P~ can may cause a workload imbalance, while using 2-DSP to generate c̄as in Pca may cause a workload imbalance. Therefore, we use two different methods for different methods.

Table 3
Summary of Methods

<table>
<thead>
<tr>
<th>Methods</th>
<th>Partition way</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-DSP</td>
<td>CA --&gt; TaskA s</td>
<td></td>
</tr>
<tr>
<td>2-DSP</td>
<td>CA --&gt; TaskA s</td>
<td></td>
</tr>
<tr>
<td>A-DSP(Our)</td>
<td>CA (\rightarrow) TaskA s</td>
<td></td>
</tr>
</tbody>
</table>

![Fig. 2](image-url)

Fig. 2. A toy example of different join models.
imbalance status. However, those $c_\alpha$s in our A-DSP model are usually carried by multiple tasks, which can smooth the workload imbalance. In other words, $c_\alpha$ in A-DSP can act as a cushioning layer for workload imbalance. This characteristic is similar to that of task grouping in [12]. Fig. 2c shows that $P_{\alpha A}^C$ takes $c_{\alpha 1}$ and $c_{\alpha 2}$ as $CA$. Then, $P_{\alpha A}$ in Fig. 2d takes $c_{\alpha 2}$ as $c_{\alpha 1}$ and splits it into four TaskA S, takes $c_{\alpha 2}$ as $c_\alpha 2$ and splits it into two TaskA S. Compared with 2-DSP, this scheme consumes less resources (6 task instances) while ensuring each task workload no excess the ideal workload. However, there may be another partition manner which consumes 4 tasks, i.e., Fig. 5, and that is what we are after. Next, we are ready to define the optimization goal of our A-DSP.

2.3 Optimization Goal
For $c_\alpha$, its resource cost includes Memory, Network and CPU, which can be modeled as follows: Memory. Since tuples are duplicated along rows or columns in $P_{\alpha A}$, values of $\alpha^a$ and $\beta^a$ in $c_\alpha$ determine the memory consumption $C_m$ considering the join operation, defined as

$$C_m = |c_\alpha^a| \cdot \beta^a \cdot R_{\text{state}} + |c_\alpha^a| \cdot \alpha^a \cdot S_{\text{state}},$$

(1)

where $R_{\text{state}}$ and $S_{\text{state}}$ are the state sizes in stream $R$ and $S$, respectively.

Network. When we duplicate the tuples along rows or columns, it consumes the network bandwidth $C_n$, which is the total communication cost of data transmission among tasks.

$$C_n = |c_\alpha^a| \cdot \beta^a \cdot R_{\text{tuple}} + |c_\alpha^a| \cdot \alpha^a \cdot S_{\text{tuple}},$$

(2)

where $R_{\text{tuple}}$ and $S_{\text{tuple}}$ are the tuple sizes in stream $R$ and stream $S$, respectively.

CPU. For theta-join, we define its computation complexity as

$$C_c = |c_\alpha^a| \cdot |c_\alpha|.$$

(3)

In general, it satisfies $R_{\text{tuple}} \propto R_{\text{state}}$ and $S_{\text{tuple}} \propto S_{\text{state}}$ [15]. Then we get $C_n \propto C_m$ based the above discussion and analysis. In other words, minimizing memory usage is equivalent to optimizing network cost. Furthermore, $C_c$ is a constant value which is $|c_\alpha^a| \cdot |c_\alpha|$ and is independent of $\alpha^a$ and $\beta^a$. Based on this, we can conclude that optimizing memory is a representative choice.

Suppose the maximum memory size for each task is $V$ and the whole tuple matrix is split into $\epsilon_c$ as $c_\alpha$. We formulate our objective as an optimization problem defined as follows:

$$\min \sum_{x \in [1:|\epsilon_c|]} \alpha^{a_{x}} \cdot \beta^{a_{x}},$$

s.t. Constraints in Def.3;

$$\forall x \in [1, \epsilon_c], \forall i \in [1, \alpha^{a_{x}}], \forall j \in [1, \beta^{a_{x}}],$$

$$|(\text{Task}A_{ij}^{c_\alpha^a})^\dagger| + |(\text{Task}A_{ij}^{c_\alpha})^\dagger| \leq V.$$

(6)

As the shown in above formulations, our optimization objective is (Exp. 4) minimizing the resource cost, while (Exp. 5) guaranteeing the correctness of processing and (Exp. 6) load balance among all task instances. In fact, under the premise of workload constraint, how to determine $CA$ to ensure the minimum task consumption is a combinatorial NP-hard problem, as it can be reduced to the Subset-sum problem [20].

3 Scheme Generation
3.1 Partition $c_\alpha$ into TaskA S
Before discussing how to partition $c_\alpha$ into TaskA S, we first introduce a theorem for guiding the formulation of partition plan.

Theorem 1. Assuming we use matrix model to handle stream join operation, if there exist $a$ and $b$ in $c_\alpha$ with $\frac{|c_\alpha^a|}{a} = \frac{|c_\alpha|}{b} = V_h$, then the processing cost for $c_\alpha^a$ or $c_\alpha$ is minimum.

Proof. Assuming the length and width of TaskA are $a (a > 0)$ and $b (b > 0)$, respectively, we have the following expression:

$$a \cdot b \leq \frac{(a+b)^2}{4}.$$ 

Equ. (7) can be modified as the following expression:

$$a + b \geq 2 \cdot \sqrt{a \cdot b}.$$ 

In the above Equs. (7) and (8), $a + b$ can be seen as the memory volume of TaskA and $a \cdot b$ represents the calculation amount. Each task has the predefined CPU and memory resources. According to Equ. (8), for the given CPU resource $C_c$ (represented by the calculation area $a \cdot b$), square $(a=b)$ has the least memory usage $C_m$. For the given memory $C_m$, square $(a=b)$ will produce the least cells and maximize the computation ability according to Equ. (7). The network cost $C_n$ can be represented by memory usage $C_m$ as declared in Section 2.3. Based on the above, we can conclude that if the length $(\frac{|c_\alpha^a|}{a})$ and the width $(\frac{|c_\alpha|}{b})$ of the subrange derived from $c_\alpha$ partition are equal, that is, equal to half of the memory size $(V_h)$, then the system consumes the least resources including CPU, memory and network.

According to Theorem 1, the numbers of row and column should be $(\frac{|c_\alpha^a|}{V_h})$ and $(\frac{|c_\alpha|}{V_h})$, respectively. Then the total number of tasks used in $c_\alpha$ can be expressed as

$$N = \left(\frac{|c_\alpha^a|}{V_h}\right) \cdot \left(\frac{|c_\alpha|}{V_h}\right).$$

Fig. 3 shows a $c_\alpha$ partition example with the stream volumes for $R$ and $S$ are $|c_\alpha^a| = 6GB$ and $|c_\alpha| = 6GB$. Given task memory $V = 10GB$ and $V_h = 5GB$, $c_\alpha$ can be divided as shown in Fig. 3b. The generated scheme in Fig. 3b takes up 4 tasks with two rows and two columns (4 divisions: $s_0$, $s_1$, $r_0$ and $r_1$).
Among those TaskA’s, we load data to rows and columns by \( V_R \) in a top-down manner. In the last row and column of \( ca \), the TaskA’s may have less data divisions compared to previous TaskA’s and are called fragment tasks filled with fragment data. In this example, TaskA\(_{00} \) is first fed by \( V_R \) for both \( ca \) and \( ca^* \) streams and then TaskA\(_{00} \) = (5GB, 5GB). However the last column and row can not be filled up. According to Equ. (9), though we can calculate the number of tasks needed for joining processing, workload are not evenly distributed among tasks because of the fragment data. Then tasks for fragment data may have free resources compared to other tasks, and it will be more obvious for the large matrix.

In order to facilitate the subsequent description, we name the two join streams as a primary stream \( P \) and a secondary stream \( D \). Then we take the primary stream \( P \) as the basis volume to calculate how much memory should be assigned for it in each task and accordingly, the secondary stream \( D \) gets the remaining portion of memory in each cell. Specifically, we use \( P_h \) to represent the number of divisions generated by primary stream, and then for the secondary stream, its division number \( D'_{y} \) can be calculated as:

\[
D'_{y} = \left[ \frac{|D|}{V - \frac{|P|}{P_y}} \right].
\]  

(10)

\( P \) may be either stream \( R \) or \( S \). We use \( N_c \) to represent the number of tasks for processing join between \( P \) and \( D \) in \( ca \) which is calculated as:

\[
N_c = P_y \cdot D'_{y} = P_y \cdot \left[ \frac{|D|}{V - \frac{|P|}{P_y}} \right].
\]  

(11)

In Fig. 3, if we take \( R \) as the primary stream \( P \) and the number of divisions generated by primary stream is \( P_y = \left\lceil \frac{|ca^*|}{V_R} \right\rceil \), then the matrix scheme of example in Fig. 3a should have only one column with two cells. However, \( D'_{y} \) calculated in Equ. (10) will have fragment tasks if its rounding up value is not equal to the rounding down value. For example in Fig. 4a, given \( V = 10GB \), \(|ca^*| = 9GB \), and \(|ca^*| = 7GB \), \( ca \) with \( \alpha = 2 \) and \( \beta = 2 \) will be generated. Since \( S \) is the primary stream, each task first gets data assignment from \( S \) by \( \frac{|ca^*|}{\beta} = 3.5GB \) and the remaining space 6.5GB can be used for divisions from \( ca^* \). The memory utilization percentage of the two tasks in the last row is 60 percent.

An optimized partition scheme of Fig. 4a is shown as Fig. 4b, which takes up only 3 tasks for \( ca^* \) \( \leftrightarrow \) \( ca \). In Fig. 4b, the replica \( |TaskA'_{01}| = 3.5GB \) of \( ca^* \) in TaskA\(_{00} \) are sent to TaskA\(_{10} \) to join with subset \( |TaskA'_{10}| = 2.5GB \) of \( ca^* \) to promise the correctness and completeness of join results. It is feasible to move tuples in \( TaskA'_{01} \) to TaskA\(_{10} \) to complete the join work for the memory threshold \( V = 10GB \) remains satisfied.

Compared to the regular matrix scheme in Fig. 4a, the optimal workload assignment in Fig. 4b can make better use of resource among tasks. Let’s take Fig. 4b to explain the generation of the irregular line, which is the last row. Given the divisions for primary stream \( S \), which is \( \beta = P_y = 2 \) in Fig. 4a, we divide those \( \alpha \) rows for secondary stream \( R \) into two types: regular ones (the first row ) and adjustive ones (the second row). For regular ones, we have \( \alpha' = D'_{y} \) lines of segments (labeled as regular in Fig. 4a), where \( D'_{y} = \left\lfloor \frac{|D|}{V - \frac{|P|}{P_y}} \right\rfloor \).

By using these regular division, we may not manage all the workload for secondary stream \( R \), since \( D'_{y} \cdot (V - \frac{|P|}{P_y}) \leq |D| \). For the remaining loads \( D'_{y} \) from \( D \) calculated as Equ. (12), it is expected to add additional \( P_h \) (as in Equ. (12)) number of columns along the last row with \( P_h < P_y \).

\[
D_L = |D| - D'_{y} \cdot \left( V - \frac{|P|}{P_y} \right),
\]

\[
P_h = \left\lceil \frac{|P|}{|D| - D'_{y}} \cdot V \right\rceil.
\]  

(12)

The difference from previous regular matrix is that we will not add one whole row (column) of tasks for the join work with the purpose of making full use of system resources. Accordingly, the optimal number of tasks \( N_o \) for \( R > \beta \) \( S \) can be calculated as:

\[
N_o = \begin{cases} 
P_y \cdot D'_{y}, & |D| = D'_{y} \cdot (V - \frac{|P|}{P_y}), \\
P_y \cdot D'_{y} + P_h, & \text{otherwise}.
\end{cases}
\]  

(13)

As described in Theorem 1, we use \( V_R \) as the divisor to find \( P_y \) for generating an optimal scheme by probing all four cases. Specifically, we make \( P_y \in \{ \left\lfloor \frac{|ca^*|}{V_R} \right\rfloor, \left\lceil \frac{|ca^*|}{V_R} \right\rceil, \left\lfloor \frac{|ca^*|}{V_R} \right\rfloor, \left\rceil \frac{|ca^*|}{V_R} \right\rceil \} \) in Equ. (13).

The algorithm of finding an optimal partition scheme is described in Algorithm 1. First, the minimal number of tasks is determined in line 1 according to Equ. (13), by enumerating all the case of round up and down; then in line 2 \( \sim \) 5, the number of rows \( \alpha \) and columns \( \beta \) can be calculated according to values of \( P \) and \( P_y \). If \( P_y \in \{ \left\lfloor \frac{|ca^*|}{V_R} \right\rfloor, \left\lceil \frac{|ca^*|}{V_R} \right\rceil \}, \) \( R \) is the primary stream, or else \( S \) is the primary one. The scheme of varietal matrix generated from Algorithm 1 can be expressed as \( \langle \alpha, \beta, P_h, + \rangle \) which means that the varietal matrix has \( \alpha \) rows, \( \beta \) columns and has \( P_h \) additional cell in \( + (r \in row, column) \).

**Algorithm 1. Partition ca to TaskA s**

**input:** Stream \( ca^* \), Stream \( ca^* \), Memory size \( V \)

**output:** Row number \( \alpha \), Column number \( \beta \), additional cells \( P_h \), additional position +

1. \( N_o \leftarrow \) Get the minimum task consumption according to Equ. (13) where \( P_y \in \{ \left\lfloor \frac{|ca^*|}{V_R} \right\rfloor, \left\lceil \frac{|ca^*|}{V_R} \right\rceil, \left\rceil \frac{|ca^*|}{V_R} \right\rceil, \left\rceil \frac{|ca^*|}{V_R} \right\rceil \} \)

2. if \( P_y \in \{ \left\lfloor \frac{|ca^*|}{V_R} \right\rceil, \left\lceil \frac{|ca^*|}{V_R} \right\rceil \} \) then

3. \( \alpha \leftarrow P_y, \beta \leftarrow D'_{y}, P_h \leftarrow N_o - P_y \cdot D'_{y} + -\) column

4. else

5. \( \alpha \leftarrow D'_{y}, \beta \leftarrow P_y, P_h \leftarrow N_o - P_y \cdot D'_{y} + -\) row

6. return \( \alpha, \beta, P_h, + \)
We still use Fig. 4b to explain Algorithm 1. According to Equ. (12), Equ. (13) and line 1 in Algorithm 1, $S$ is the primary stream and $R$ is the secondary one, in which $\beta = 2$, $D_j^L = \frac{9}{35} \cdot 72 = 1$. TaskA$_{00}$ and TaskA$_{01}$ are supposed to have regular workload assignments with $3.5\text{GB}$ from ca', and the remaining memory is used for ca'', which will be $10 - 3.5 = 6.5\text{GB}$. Since ca' has load more than $6.5\text{GB}$, we add one more row which is the adjustable division for the remaining data of ca' that $D_j^L = 9 - 6.5 = 2.5\text{GB}$. In such a case, the TaskA s in regular division lines have full usage to memory $6.5 + 3.5 = 10\text{GB}$ as in TaskA$_{00}$ and TaskA$_{01}$. For adjustable purpose, we add $P_k = 1$ TaskA to join the remaining data $D_j^L$ in R with $S$, which belongs to TaskA TaskA$_{10}$ and TaskA$_{11}$ in Fig. 4a. In this adjustable row, $D_j^L$ will join with the subset of ca' for TaskA$_{10}$ and TaskA$_{11}$ (3.5GB) and then the workload in TaskA$_{10}$ comes to be 9.5GB. The varietal matrix scheme shown in Fig. 4b can be expressed as $<1, 2, 1, \text{row}>
$. 

**Theorem 2.** Algorithm 1 will consume less tasks than using Theorem 1 directly and ensure the correctness of operation when using matrix model for ca' $\propto$ ca'' with the memory size of each task V.

**Proof.** Assume that there exists another varietal matrix $M'$ with scheme $<a'\beta, P_j, t^+>$, and the number of tasks $N'$ used in $M'$ is smaller than $N$. To find the smaller $N$ or, Algorithm 1 tries all possible values that make $|p|_p$ nearest to $V_b$ according to Equ. (12), Equ. (13) and line 1. In other words, it is impossible for $\frac{|q|_q}{p}$ and $\frac{|p|_p}{q}$ to get closer to $V_b$ than $\frac{|q|_q}{p}$ and $\frac{|p|_p}{q}$. According to Theorem 1 that squared cell shape consumes the minimal resources, the assumption of existing regular matrix $M'$ does not hold. □

### 3.2 Partition $\bar{C}$ into $\tilde{c}$a s (ca s)

In this subsection, we introduce a heuristics algorithm to accomplish the optimization problem with theoretical perspectives. Specifically, here we present how A-DSP provides a theoretical guarantee upper-bound for task consumption to partition $\bar{C}$ into $\tilde{c}$a s (ca s). Using tuple matrix model to handle $\theta$-join, a key observation is that the distribution of $CA$ has the feature of Monotonicity. The monotonicity can be expressed as if $c_{(i,j)}$ is not a result cell, then either all cells $(k, l)$ with $k \leq i$ and $l \geq j$, or all cells $(k, l)$ with $k \geq i$ and $l \leq j$ are also not result cells [10], [13]. It should be pointed out that the "\#" operation is not monotonic, for its operation semantic making each cell in $C$ become a potential result. In such cases, our A-DSP model will adaptively adopt the 2-DSP architecture, which can be reflected from Algorithm 2 later. Next, we define a partition way for $CA$ as follows.

**Definition 5.** Splitting the area $\bar{c}a$ into two sub-areas: $\bar{c}a^d$ and $\bar{c}a_d$, if $\bar{c}a^d \cup \bar{c}a_d = \bar{c}a$ and $\bar{c}a^d \cap \bar{c}a_d = \emptyset$, we call this area partition action as $\bar{c}a$'s area dichotomy, denoted as AD($\bar{c}a$).

Based on the above Definition 5, we call $d$ as the split point and the minimum task consumption of $CA$ based on area dichotomy can be expressed as:

$$N^\text{AD}(CA) = \min_{d \in CA_D} \{N^\text{AD}(\bar{c}a^d) + N^\text{AD}(\bar{c}a_d)\},$$

(14)

where $CA_D$ is the universal set of split point in $\bar{c}a$. Equ. (14) is an iteration expression to enumerate all split scheme to find the minimal task consumption. Thus, we have the following theorem.

**Theorem 3.** Among all schemes generated by $\bar{c}a$'s area dichotomy, Equ. (14) can denote the one which with minimum task consumption.

**Proof.** Assume there is a partition scheme with the set of split point $\{d_i\}$, where $d_i$ is the split point of the $i$th iteration partition, and $N_{\min}$ is the task consumption by this partition scheme. If $N_{\min} < N^\text{AD}(CA)$, then we have $\{d_i\} \notin \bar{c}a_D$, which contradicts to the assumption that $CA_D$ is the universal set of split point in $CA$ in Equ. (14). □

Essentially, Equ. (14) is a combinatorial mathematics problem and its iteration times is a Catalan number [21]. Directly adopting an exhaustive enumeration method to obtain the partition scheme will undoubtedly incurs the high computational complexity, reaching up to $O(\frac{\sqrt{c_{AD}}}{c_{AD}^2})$. Therefore, we define an iteration termination condition as follows.

**Definition 6.** Using area dichotomy to split the coverage area $\bar{c}a$ into two sub-areas $\bar{c}a^d$ and $\bar{c}a_d$, the iteration termination condition is $\forall d \in \bar{c}a_D, N^{\bar{c}a^d} \geq N^{\bar{c}a_d} + N^{\bar{c}a_d}.$

Algorithm 2 lists the steps of $\bar{c}a$ partition based on the above discussions. At the initialization stage of Algorithm 2, the matrix is generated by the Cartesian produce of the two join streams. First, it finds the split point according to Definition 5 in line 4. Second, Algorithm 2 judges whether to stop the iterative process, and gathers the corresponding split results in lines 5 ~ 10. Finally, it picks out the partition result which with the minimal task consumption as its output in line 11. We continue using the example in Fig. 2 to illustrate Algorithm 2, and the partition result is shown in Fig. 5. Algorithm 2 takes the whole tuple matrix $C$ as iterative entry and splits it into two areas: $\bar{c}a_1 = \{c_{(6,6)}(c_{1,11}, c_{5,5})\}$ and $\bar{c}a_2 = \{c_{(6,6), c_{12,12}}\}$, using area dichotomy. For $\bar{c}a_1$, Algorithm 2 stops splitting it because the continuing split action can not reduce task consumption. Due to $N^{\bar{c}a_2} = 4$ and $N^{\bar{c}a_2} = 2$, Algorithm 2 picks the fewer tasks consumption scheme by splitting $\{c_{6,6}, c_{12,12}\}$ into two sub-areas. Finally, Algorithm 2 generates a scheme that consumes 4 tasks.
Algorithm 2. Partition $C$ to $ca$ s

input: $C$
output: $ca$ s
1: $ca ← CA$
2: function PartitionArea($ca$)
3: /\* $E_i/\*E_{i+1}$ : the beginning/ending cell of $ca$*/
4: foreach $c_{(i,j),} e_{(i,j)}$ in $ca$ do
5: if $[c_{(i,j)}, e_{(i,j)}] \cup [c_{(j,j)}, e_{(j,j)}] = ca$ and $[c_{(i,j)}, e_{(i,j)}] \cap [c_{(j,j)}, e_{(j,j)}] = \emptyset$ then
6: /*According to Definition 5*/
7: if $N[c_{(i,j)}, e_{(j,j)}] + N[e_{(i,j)}, e_{(j,j)}] < N^\alpha$ then
8: else
9: $cas_{(i,j)} ← [c_{(i,j)}, e_{(i,j)}]$
10: /* $cas_{(i,j)}$ : the set of coverage area be derived from the first iteration, $CAS$: the set of $cas_{(i,j)}$*/
11: get $ca$ s ($cas \in CAS$) with the minimal $\sum_{cas \in CAS} N^\alpha$
/* According to Theorem 3*/
12: return $ca$ s

Next, we discuss the task consumption upper-bound of Algorithm 2.

Definition 7. Given area $ca$, suppose there is a minimum task consumption $N^\alpha_1$, and the task consumption by Algorithm 2 is $N^\alpha$, we refer to the ratio of $N^\alpha/N_2$ as consumption coefficient, denoted by $\xi$.

Lemma 1. For the area $ca$ with $\alpha^\alpha \geq 2$ and $\beta^\alpha \geq 2$, if Algorithm 2 stops splitting it, then the cell set $RCC$ in $ca$, where

$$RCC = \left\{ c_{(i,j)} \left| \left( (\alpha^\alpha - 1) \cdot V_h + 1 \geq k \geq V_h, (\beta^\alpha - 1) \cdot V_h + 1 \geq t \geq V_h \right) - c_{(\alpha^\alpha - 1), \beta^\alpha \cdot \beta^\alpha - 1, \beta^\alpha - 1} \right. \right\},$$

should be all the result.

Proof. To verify in the worst case, we use the naive method to measure the task consumption according to Eq. (9), where $N^\alpha = \alpha^\alpha \cdot \beta^\alpha = \left[ \frac{\alpha^\alpha}{\beta^\alpha} \right] \cdot \left[ \frac{\beta^\alpha}{\alpha^\alpha} \right]$. The formation of $RCC$ can be accumulated in three steps:

Step-1 (According to Definition 6): The precondition of Lemma 1 that Algorithm 2 stops splitting area $ca$ means $\forall d \in ca_d$, $N^\alpha_d < N^\alpha_{ca_d} + N^\alpha_{ca_d}$. Then, the cells $\left\{ c_{(i,j)} \left| k \cdot V_h = 0, l \cdot V_h = 0, k \neq |\alpha^\alpha|, l \neq |\beta^\alpha| \right. \right\}$ (e.g., the red cells in Fig. 6) are definitely not split points, otherwise, the scheme cannot be the worst case among all partition schemes. They should be contained by $RCC$.

Step-2 (According to Definition 5): Due to the fact that area dichotomy splits the area $ca$ into two sub-areas and $c_{(i,j)}$ in $ca$ is not a split point, then, existing cells $c_{(i,j)}$ and $c_{(j,j)}$ both result. Based on this, the cells in $RCC$ are expanded to

$$\left\{ c_{(i,j)}, c_{(i,l+1), c_{(k+1,j)}}, k \cdot V_h = 0, l \cdot V_h = 0, k \neq |\alpha^\alpha|, l \neq |\alpha^\alpha| \right\}.$$

Step-3 (According to monotonicity): The monotonicity defines that the cell(s) between result cells are also results.

Combining this, the result cells $RCC$ can be expressed as

$$\left\{ c_{(i,j)} \left| (|\alpha^\alpha - 1| \cdot V_h + 1 \geq k \geq V_h, (|\beta^\alpha - 1|) \cdot V_h + 1 \geq t \geq V_h \right) - c_{(\alpha^\alpha - 1), \beta^\alpha - 1, \beta^\alpha - 1} \right\},$$

which equivalents to the description of Lemma 1 (surrounded by blue dotted line in Fig. 6).

Then, the upper-bound of $\xi$ can be expressed as follows:

Theorem 4. Using Algorithm 2 to partition $C$ can ensure an upper-bound of its task consumption: $\xi \leq \frac{\alpha^\alpha \cdot \beta^\alpha}{\alpha^\alpha \cdot \beta^\alpha - \alpha^\alpha - \beta^\alpha + 1}$, where $\alpha^\alpha \geq 2$ and $\beta^\alpha \geq 2$.

Proof. According to Lemma 1, the minimal task consumption is consisted of three parts: $c_{(i,j)}$(ca), $c_{(V_h, V_h)}$ consumes 1 task,

$$\left| c_{(V_h+1, V_h+1), c_{(\alpha^\alpha - 1, \beta^\alpha - 1, \beta^\alpha - 1)} \right| \text{ consumes } (\alpha^\alpha - 1) \cdot (\beta^\alpha - 1) \text{ task(s) and } \left| c_{(\alpha^\alpha - 1, \beta^\alpha - 1, \beta^\alpha - 1)} \cdot c_{(R,S)} \right| \text{ consumes 1 task}. $$

Then, we have $N_2^\alpha \geq 1 + (\alpha^\alpha - 1) \cdot (\beta^\alpha - 1) + 1$. Since $\xi = \frac{\alpha^\alpha \cdot \beta^\alpha}{\alpha^\alpha \cdot \beta^\alpha - \alpha^\alpha - \beta^\alpha + 1}$, we have $\xi \leq \frac{\alpha^\alpha \cdot \beta^\alpha}{\alpha^\alpha \cdot \beta^\alpha - \alpha^\alpha - \beta^\alpha + 1}$. Making $C$ as $ca$, Theorem 4 is verified.

The statement of Theorem 4 gives an estimation or hint on the worst case of task consumption. However, just as the unique distribution shown in Fig. 6, the probability of a worst case scenario is negligible, which can be validated by the experimental results in Section 5. Algorithm 2 uses area dichotomy to split the coverage area $ca$ into two sub-areas $ca_d$ and $ca_d$, and its iteration termination condition is $\forall d \in ca_d$, $N^\alpha_d \geq N^\alpha_{ca_d} + N^\alpha_{ca_d}$, its computational complexity is not more than $T(c_{\alpha^\alpha} \cdot c_{\beta^\alpha})$, where $T(\alpha \cdot \beta) \cdot \alpha \cdot \beta$ is $\kappa$. $T(c_{\alpha^\alpha} \cdot c_{\beta^\alpha})/2 + O(\alpha \cdot \beta)$, as illustrated in Fig. 6 and Theorem 4, the cells $\{ c_{(i,j)} \left| k \cdot V_h = 0, l \cdot V_h = 0, k \neq |\alpha^\alpha|, l \neq |\alpha^\alpha| \right. \}$ (the four red cells in Fig. 6) are definitely not split points, then $\kappa = 4$ and $T(c_{\alpha^\alpha} \cdot c_{\beta^\alpha}) = O((\alpha \cdot \beta)^2).$

4 IMPLEMENTATION
The adaptive processing architecture is shown in Fig. 7 and can be decomposed into the following five steps: Step-1: Monitoring workload. It collects information about the tuple matrix and the space occupied by the two join streams, and the task consumption of the existing processing scheme. On receiving the reporting information, the controller first evaluates the number of task consumption according to Algorithm 1 and Algorithm 2. Step-2: Generating processing scheme. It produces a new scheme according to workload...
and resource information, as presented in Section 3; Step-3: Making task-load mapping. It expects to find the task-load mapping function so as to maximize non-moving data volume when transforming from the old scheme to the new scheme. This step will be described in Section 4.2. Step-4: Generating migration plan. It schedules the data migration among tasks according to task-load mapping scheme. This step will be described in detail in Section 4.3. Step-5: Defining consistent protocol according to migration plan. This step defines consistent protocols to ensure the correctness of system.

We omit the detailed description of step-5 in this paper since it is same as [11]. Moreover, the implementation process of our model should include two phases: \( P_{CA} \) (partition \( CA \) into \( CA \) s) and \( P_{Co} \) (partition \( CA(\text{ca}) \) into \( TaskA \) s). After the final scheme generated by Algorithms 1 and 2, the workload adjustment strategy among \( ca \) s is a key-based issue which has been explored in our previous work [22], so that will not be reiterated in this paper. Due to the fact that the routing strategy is the essential step for the incoming stream, we first introduce it in the following subsection.

### 4.1 Routing Strategy

In view of our A-DSP model is a composite structure, its routing strategy includes two layers as listed in Algorithm 3.

#### Algorithm 3. Routing Strategy Algorithm

**input:** Input tuple: \( r \), Mapping function: \( F \)

**output:** Routing destination RD: \( \{(ca, \downarrow, th)\} \)

1. \( k \leftarrow E(r) \) / * extract the key of tuple \( r \*) /
2. / * * * Step-1: Routing tuples in \( \tilde{C} \) **/ /
3. \( C_0 \leftarrow \text{RoutingIn}(\tilde{C}, k, F) \) / * \( C_0 \) is the set of \( ca \) **/ /
4. / * * * Step-2: Routing tuples in \( ca \) **/ /
5. \( RD \leftarrow \text{RoutingIn}(Ca, \uparrow) \)
6. return RD
7. function \( \text{RoutingIn}(\tilde{C}, k, F) \)
8. \( K^* \leftarrow F(k) \)
9. foreach \( k^* \in K^* \) do
10. \( x \leftarrow \text{BasicPartition}(k^*), Ca \leftarrow ca^2 \)
11. return Ca
12. function \( \text{RoutingIn}(Ca, \uparrow) \)
13. foreach \( ca^2 \in Ca \) do
14. if \( \uparrow \in R \) then
15. \( \downarrow \leftarrow \text{row}, th \leftarrow \text{RandomInt}[0 \sim (a_{ca^2} - 1)] \)
16. else
17. \( \downarrow \leftarrow \text{column}, th \leftarrow \text{RandomInt}[0 \sim (b_{ca^2} - 1)] \)
18. \( RD \leftarrow (ca^2, \downarrow, th) \)
19. return RD

### Table 4

<table>
<thead>
<tr>
<th>Notations</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( m_{ij} )</td>
<td>task instance corresponding to ( TaskA_{ij} )</td>
</tr>
<tr>
<td>( h_{ij}^R / h_{ij}^S )</td>
<td>the sub-stream ( R / S ) that has been stored in ( m_{ij}^c ), represented as a range ([b, c])</td>
</tr>
<tr>
<td>( M_m / M_n )</td>
<td>old task matrix and new task matrix for ( ca )</td>
</tr>
<tr>
<td>( k / l )</td>
<td>( k )th row and ( l )th column in new scheme</td>
</tr>
<tr>
<td>( h_{ij}^R / h_{ij}^S )</td>
<td>data has been stored in ( m_{ij} ) in ( ca )</td>
</tr>
<tr>
<td>( s_{ij}^R / s_{ij}^S )</td>
<td>data for ( m_{ij} ) in new scheme ( M_i ) in ( ca ), represented as a range ([b, c]) on stream ( ca^2 / ca^1 )</td>
</tr>
<tr>
<td>( tpi )</td>
<td>the mapping of tasks between old and now scheme</td>
</tr>
<tr>
<td>( mp )</td>
<td>the migration plan</td>
</tr>
<tr>
<td>( TP/MP )</td>
<td>the set of ( tpi/mp )</td>
</tr>
</tbody>
</table>

**Step-1:** Routing tuples in \( \tilde{C} \). This step is responsible for routing tuples into \( ca \)s. To ensure that one tuple could be sent to various destinations, here using a content-sensitive manner, which according to a basic mapping function \( F(k) \). To this end, Algorithm 3 first extracts the join key from each incoming tuple in line 1. Then it figures out which key(s) the tuple should pair in line 8. According to the pair key, Algorithm 3 generates the destination(s) for the incoming tuple, based on a basic routing function (e.g., consistent hash) in lines 9–11.

**Step-2:** Routing tuples in \( ca \). This step is responsible for determining which task(s) in \( ca \) is(are) destination(s). Algorithm 3 first identifies which stream the inputting tuple comes from in lines 14 ~ 17. Accordingly, all task(s) in the row or column are selected as destination(s) in line 18. In Algorithm 3, the destination is denoted by \( (ca, \downarrow, th) \), means the input tuple should be send to all tasks located at \( \downarrow \) in \( ca \) and \( th \in N \) in \( ca \) in line 18.

In example of Fig. 2d, for the tuple from stream \( S \) and with join key 18, Algorithm 3 first determines the first \( ca(ca1) \) is its direction, which according to the join predicate expression \( (R \cdot k - S \cdot k) \leq 2 \) and storage strategy (i.e., \( \{k_1 \sim k_2\} \rightarrow ca1, \{k_2 \sim k_3\} \rightarrow ca2 \) ). Since \( ca1 \) has two columns, Algorithm 3 randomly selects the 0th column as its destination line (i.e., destination is \( ca1, column, 0 \) ) in Algorithm 3.

### 4.2 Scheme Changing

There are two criteria which should be guaranteed during the process of \( ca \)’s scheme changing. The first one is to ensure the correctness of process and the second one is to lower migration cost during the process of scheme changing as far as possible. To simplify our description, some additional notations used in the following sections are summarized in Table 4.

We now use \( m \) and \( M \) to denote task instance and task matrix respectively, and \( m_{ij} \) corresponding to calculation area \( TaskA_{ij} \) in \( ca \). Furthermore, we use \( m_{ij} \) and \( m_{kl} \) to represent the task instance in \( M_o \) and \( M_n \) respectively, where \( i(k) \) and \( j(l) \) are the row number and column number of \( M_o \) (\( M_n \)). We define the correlation coefficient \( \lambda_{ij}^{mk} \) to reflect the volume of data overlap between \( m_{ij} \) and \( m_{kl} \), which can be calculated as \( \lambda_{ij}^{mk} = |h_{ij}^R \cap s_{kl}^R| + |h_{ij}^S \cap s_{kl}^S| \).
Algorithm 4. Task Mapping TP Generation

input: Old task matrix scheme $M_o$, New task matrix scheme $M_n$
output: Task mapping set TP

1: foreach $m_{ij}$ in Old scheme $M_o$ do
2:     foreach $m_{kl}$ in New scheme $M_n$ do
3:         $\lambda_{ij}^o := (h_{ij}^o \cap s_{kl}^o) \cdot |ca^o| + (h_{ij}^o \cap s_{kl}^o) \cdot |ca^o|$
4:         $TP_i \leftarrow \langle m_{ij}, m_{kl}, \lambda_{ij}^o \rangle / *TP_i$ is a temp set /*
5:     Initialize $TP = \emptyset$
6:     foreach $tp_{i}$ in $TP$ in descending order based on $\lambda_{ij}^o$ do
7:         if $m_{ij}$ or $m_{kl}$ in $tp_{i}$ has been appeared in $TP$ then
8:             Continue
9:         $\langle m_{ij}, m_{kl} \rangle \rightarrow TP$
10:     return TP

Algorithm 4 shows the task mapping method, which aims to minimize the states migration when using the new scheme $M_n$. Specifically, Algorithm 4 first enumerates all the possible mappings in form of $tp_{i} = \langle m_{ij}, m_{kl}, \lambda_{ij}^o \rangle$ as shown in lines (1 $\sim$ 4); then it selects the optimal mappings which have larger $\lambda_{ij}^o$ among all mapping sets in lines (6 $\sim$ 10). Task mapping $TP$ generated by Algorithm 4 gathers the largest cumulative values of $\lambda_{ij}^o$. Because each $m_{ij}$ or $m_{kl}$ appears in $TP$ only once at most, then the correlation coefficient $\lambda_{ij}^o$ is independent of others. Our algorithm always selects the mapping pair with biggest $\lambda_{ij}^o$, and then it will generate the maximum cumulative value of $\lambda_{ij}^o$. In other words, Algorithm 4 finally produces the minimal migration cost during the process of scheme changing.

Considering scheme generation in Section 3 and task mapping generation discussed above, we design an advanced scheme mapping for reducing migration cost. In order to make it easy for explanation, we take a one dimension scheme division as an example and treat its total volume as unit "1", shown in Fig. 8, where $h_i(s_i)$ represents the range processed by task $i$.

A naive method is to divide the stream into even ranges and assign each range to one task as shown in Fig. 8a. In old scheme, there are 4 tasks (No.0$\sim$3) and each task manages 25 percent percentage of the whole stream, represented as $h_i$ ($i \leq 3$). When it is scaled out to 5 tasks, 5 ranges are generated evenly and each range $s_j$ ($j \leq 4$) maps to one task. Based on Algorithm 4, we can figure out the best mapping from $\{h_i\}$ to $\{s_j\}$ shown in Fig. 8a, represented by the dotted line. The shadowed range in old scheme will be migrated among tasks, and the newly added task will be assigned the data in range $[2/5, 3/5]$ labeled as $s_4$. The total volume of data migration is $\frac{1}{15} + \frac{1}{15} + \frac{1}{15} = \frac{1}{5}$.

Given that join correctness is independent of the order of tuples as long as we can guarantee that the same row (column) has the same states as described in Section 2. In this context, we can conduct an optimization based on start-point-alignment method for task mapping as follows. We first align the same range start points for $\{s_j\}$ in new scheme to those from $\{h_i\}$ in old scheme, if any. In Fig. 8b, the old scheme is scaled out to 5 tasks. We align the same start range points between 4 tasks such as $s_0 \sim s_3$ from the new scheme and $h_0 \sim h_3$ from the old scheme. Each $h_i$ cuts down the shadowed $1/20(=1/4 - 1/5)$ of the range and moves them to the newly inserted task that is $s_4$. In such a case, the total migration volume is $\frac{1}{15} + \frac{1}{15} + \frac{1}{15} + \frac{1}{15} = \frac{1}{5}$, which is less than the migration cost generated by

4.3 Migration Plan Generation

Figuring out the part of data which should be migrated among tasks is a necessary information in the process of scheme changing. We use $\bullet$ to represent the join stream that $\bullet \in \{ca^o, ca^o\}$ and $n_{ij}^m$ means the data that are lacked in $m_{ij}$, and then the range of data $n_{ij}^m$ is:

$$n_{ij}^m = s_{ij}^m - (s_{ij}^m \cap h_{ij}^o).$$

Then we define the migration plan as $mp = \langle m_{ij}, m_{kl}, n_{ij}^m \rangle$ that can be read as: for stream $\bullet$, the data $\bullet$ should be copied for $m_{ij}$ in old scheme $M_o$ to $m_{kl}$ in new scheme $M_n$, where $\bullet$ is:

$$\bullet = h_{ij}^o \cap n_{ij}^m,$$

For each $m_{kl}$, we use $d_{kl}$ to represent the data which no longer needed and should be moved out, and $d_{kl}$ can be calculated as:

$$d_{kl} = h_{ij}^o \cap n_{ij}^m,$$

In this case, the migration plan can be represented as $mp = \langle \bullet, m_{ij}, d_{kl} \rangle$. The migration plan with mark $\odot$ can be read as: for stream $\bullet$, delete data $d_{kl}^\bullet$ from $m_{ij}$.

The generation of migration plan is described in Algorithm 5 and can be divided into four steps as follows: Step-1: Discarding states that are no longer needed in $M_o$. As shown in line 1 of Algorithm 5, this step is used to clean useless states generated by old scheme $M_o$. Specifically, some states will be discarded when scheme change happens. Step-2: Filling stream data for task instances in the new scheme. We can get the whole data set in stream $R$ or $S$ by combining the data from the first row or the first column in $M_o$. As in line (2 $\sim$ 11), we can fill each task instance with data in $m_{kl}$ using tuples which are stored in the first row or column in $M_o$. Step-3: Handling the last row or column with irregular scheme. This step plays the role that making scheme full use of resources. It redistributes the subset of data of primary stream located in task instances $P_8 \sim P_9$ in lines (12 $\sim$ 18). Step-4: Deleting useless tuples. It deletes data with $\odot$ mark in $mp$ under the new scheme $M_n$ in lines (19 $\sim$ 21).

In above steps, step-1 will be triggered when the old scheme $M_o$ is an irregular matrix and step-3 will be triggered when the new scheme $M_n$ is irregular. To make it comprehensible, we first walk through an example with regular scheme transformation (just use step-2 and step-4 in Algorithm 5) and then discuss the details of the irregular scheme generation.
Algorithm 5. Migration Plan Generation

**input:** Old scheme $M_o$, New scheme $M_n$, Task mapping $TP$  
**output:** Migration plan $MP$

1: Discard states with mark $\Box$ for each task in new scheme
2: **foreach** row $i$ with column 0 in old scheme $M_o$ **do**
3:   **foreach** task $m_{i0}$ in new scheme $M_n$ **do**
4:     **if** $h_{i0}^R \land n_{i0}^R \neq \emptyset$ **then** / * According to Equ.(15) & 16 * /
5:       $<m_{i0}, m_{i1}, h_{i0}^R \land n_{i0}^R> \rightarrow MP$
6:     **end if**
7:   **end foreach**
8: **end foreach**
9: **foreach** column $j$ with row 0 in old scheme $M_o$ **do**
10:   **foreach** task $m_{i0}$ in new scheme $M_n$ **do**
11:     **if** $h_{i0}^R \land n_{i0}^R \neq \emptyset$ **then**
12:       $<m_{i0}, m_{i1}, h_{i0}^R \land n_{i0}^R> \rightarrow MP$
13:     **end if**
14: **end foreach**
15: **end foreach**
16: **end foreach**
17: **foreach** task $m_{i2}$ in new scheme $M_n$ **do**
18:     **if** $P = R$ **then** / * $y \in [0, P - 1]$ * /
19:       $<\Box, m_{i2}, s_{i2}^D > \rightarrow MP$
20:     **end if**
21: **end foreach**
22: **return** $MP$

A scheme changes from $2 \times 2$ to $2 \times 3$ as depicted in Fig. 9a, and we also treat the total volume of $ca^f/\bar{ca}^a$ as unit $"V"$. In old scheme $M_o$, each task manages half size of stream data from $ca^f$ and $\bar{ca}^a$ shown in Fig. 9a: each row manages half size of $ca^f$ with $h_{i0}^R = h_{i0}^R = [0, 1]$ and $h_{i0}^R = h_{i0}^R = [0, 1]$, each column manages half size of $\bar{ca}^a$ with $h_{i0}^R = h_{i0}^R = [0, 2]$ and $h_{i0}^R = h_{i0}^R = [0, 1]$. When the workload of stream $\bar{ca}^a$ increases, system may scale out by adding one more column with two tasks using a $2 \times 3$ scheme as shown in Fig. 9b. In this case, data partitions to $ca^f$ are unchanged where tasks in the first row still manage half size of volume ($s_{i1}^D = [0, 1], i \in \{0, 1, 2\}$) and tasks in the second row manage the other half ($s_{i1}^D = [0, 1], i \in \{0, 1, 2\}$). Stream $ca^a$ should be split into three partitions for three columns, each of which manages $\frac{1}{3}$ range of data, that is $s_{i0}^D = [0, \frac{1}{3}], s_{i1}^D = [\frac{1}{3}, \frac{2}{3}]$, and $s_{i2}^D = [\frac{2}{3}, 1], i \in \{0, 1\}$.

According to the discussion in Section 4.2, if we have the optimal partitioning scheme with minimal migration cost, $TP$ is $<m_{i00}, m_{i01}, m_{i02}, m_{i10}, m_{i11}, m_{i12}>$. In Fig. 9b, we pair the relevant tasks between $M_o$ and $M_n$ by assigning the same numbers for tasks. The tasks tagged with red numbers $\Box$ and $\Box$ in $m_{i01}$ and $m_{i11}$ are not paired. $m_{i01}$ is supposed to manage data $n_{i01}^R = [0, \frac{1}{3}]$ and $n_{i11}^R = [\frac{1}{3}, \frac{2}{3}]$. $m_{i11}$ is supposed to manage data $n_{i11}^R = [\frac{2}{3}, 1]$ and $n_{i11}^R = [\frac{2}{3}, 1]$. According to Algorithm 5, in $m_{i01}$, $s_{i01}^D$ is generated by duplicating $ca^f$ from $m_{i00}$. Since $ca^a$ is reallocated by splitting into 3 parts for the insertion of a new column, it first generates the complete data set by combining $h_{i00}^S$ and $h_{i00}^S$ in scheme $M_o$ and then $s_{i01}^D$ is generated by replicating $ca^a$ data from $m_{i00}$ with $h_{i01}^S$ by range $[0, \frac{1}{3}]$ and from $m_{i10}$ with $h_{i01}^S$ by range $[\frac{2}{3}, 1]$. Then the data for $s_{i01}^D$ is deleted from these task instances. $m_{i11}$ in $M_n$ will be assigned data in the same way as $m_{i01}$ does.

5 EVALUATION

5.1 Experimental Setup

Environment. We implement the approaches and conduct all the experiments on top of Apache Storm [23]. The Storm system is deployed on a cluster of 21 HP blade instances, each of which runs CentOS 6.5 operating system and is equipped with two Intel Xeon processors (E5335 at 2.00GHz) with four cores and 32GB RAM. Overall, there are 300 virtual machines available exclusively for our experiments, each with dedicated memory resources of 2GB.

Data Sets. We test the proposed algorithms using two types of data sets. The first TPC-H data sets is generated by the dgen tool shipped with TPC-H benchmark [24]. Before feeding the data to the stream system, we pre-generate and pre-process all the input data sets. We adjust the data sets with different degrees of skew on the join attributes under Zipf distribution by choosing a value for skew parameter $\alpha$. By default, we set $\alpha = 1$. The second data set is 10GB social data1 (coming from Weibo which is the biggest Chinese social media data) which consists of 20,000,000 real feed tuples. We run self-join on social data to find the correlation degree among tuples.

Queries. We experiment on four join queries, namely one equi-join from the TPC-H benchmark and three synthetic band-joins. The equi-join, $Q_{E_{eq}}$, represents the most expensive operation in query $Q_5$ from the benchmark. $Q_{B_{NCI}}, Q_{B_{MR}}$ and Social data query are all band-joins, which are different in the range of join. Specifically, $Q_{B_{NCI}}$ is the $\theta$-join query that corresponds to a small range, while $Q_{B_{MR}}$ is the theta-join query that represents a big range. $Q_{B_{MR}}$ and Social data query are full band-joins which require each tuple from one stream meets all the tuples from the other stream. The $Q_{E_{eq}}, Q_{B_{NCI}}$ and $Q_{B_{NCI}}$ are used in [11], [12].


![Fig. 9. Stream distribution example.](image-url)
Baseline Approaches. In A-DSP, we compress the tuple matrix in our experiments using a matrix compression method proposed in [10], which generates the sample matrix having a much smaller size than the original matrix and guarantees the sample tuple matrix being high fidelity. For the purpose of comparison, we evaluate four different distributed stream join algorithms as follows.

Square [19] figures out the number of tasks through a simple and easy way defined Eqn. (9).

Dynamic [11] takes join matrix as its processing model and assumes that the number of tasks in a matrix must be a power of 2. Since the model needs to maintain its matrix structure, if the workload of one stream increases twofold, Dynamic will double cells along the side corresponding to this stream. Meanwhile, cells along the other side will get reduced by half. In addition, during system scaling out, Dynamic splits the states of every node into 4 nodes if storage of any task exceeds half of specified memory capacity.

\(\text{Readj} [15]\) is designed to minimize the load of restoring the keys based on the hash function, implemented by key rerouting over the keys with maximal workload. The migration plan of keys for load balance is generated by pairing tasks and keys. For each task-key pair, their algorithm considers all possible swaps to find the best move alleviating the workload imbalance. In Readj, \(\sigma\) is a configurable parameter, deciding which keys should take part in action of swap and move. Given a smaller \(\sigma\), Readj tends to track more candidate keys and thus finds better migration plans. In order to make fair comparison, in each of the experiment, we run \(\text{Readj}\) with different \(\sigma\)’s and only report the best result from all attempts.

\(\text{Bi}\) and \(\text{Bi}6[12]\) handle \(\theta\)-join using a complete bipartite graph. On one side of the bipartite graph, a data stream \(\mathcal{R}\) is decomposed into substreams by a key-based hash function, each partition of which is stored and maintained by a computation node. In the following part of this paper, we use \(\text{Bi}\) to represent there is only one subgroup for each side of join-biclque and \(\text{Bi6}\) to denote there are six subgroups for each side. For routing the incoming tuple, they use a two-tier architecture of the router, consisting of shuffler and dispatcher. The shuffler, implemented as a spout, ingests the input streams and forwards every incoming tuple to the dispatcher. The dispatcher, implemented as a bolt, forwards every received tuple from the shuffler to the corresponding units in the joiner to store and join.

Performance Metrics. We evaluate resource utilization and system performance through the following metrics:

- **Tasknumber** is the total number of tasks consumed by system and each task is assigned with a specified quota of memory space \(\mathcal{V}\).
- **ExecutionTime** is consumption time taken to deal with a certain amount of data.
- **Throughput** is the average number of tuples that processed by system per second (time unit).
- **Average join request account** is the average number of tuples which should be joined within each task.
- **Migration volume** is the total number of tuples which should be moved to other tasks during scheme changing.
- **ResourceCost (RC)** is the cumulative usage volume of a certain resource which can be expressed as \(\text{RC} = \sum_{r \in \mathcal{R}} r \cdot t_r\), where \(r\) is the measurement of resource consumption, which may be memory, network or CPU, \(\mathcal{R}\) is the set of \(r\) and \(t_r\) is the duration time for those resource \(r\).

5.2 Full History Stream Joints

Fig. 10 demonstrates the trend on task consumption and execution time during loading all 16GB data into Storm system. The maximum input rate can be set to consume all the computing power of each task, using enough parallelism for spout in Storm.

During data loading as in Fig. 10a, our algorithm \(A\)-DSP has stable performance while Dynamic meets sharp increase in task number. This is because Dynamic has a strict requirement that the number of tasks must be a power of two, and then, Dynamic must quadruple its tasks and may waste resources when system scales out. Contrarily, our algorithm \(A\)-DSP generates the processing scheme based on current workload. Square limits the TaskA must be square shape and the divides \(\mathcal{C}\)A directly makes it use more computing resources. Since \(\text{Bi}\) is designed for memory optimization, it is obvious that \(\text{Bi}\) uses the minimal number of tasks. Specifically, \(\text{Bi6}\) sets up 6 subgroups for each stream and every subgroup contains one task initially. As data flows in, tasks inside subgroups will scale out dynamically. Figs. 10b, 10c, and 10d depict processing efficiency under different data skewness executing \(\mathcal{E}_{\mathcal{Q}}\), \(\mathcal{B}_{\mathcal{NCI}}\) and \(\mathcal{B}_{\mathcal{MR}}\). A-DSP and matrix-join methods including Square and Dynamic, can process join stably since data are distributed to tasks randomly. Although \(\text{Bi}\) takes up fewer tasks, its efficiency is almost three times lower than others due to its lack of computing resources. Specifically, when \(z = 2\), severer skewness may cause tuple broadcast among groups. \(\mathcal{B}_{\mathcal{MR}}\) is a wide range of band-join, the advantages of subgrouping in \(\text{Bi6}\) completely disappear as shown in Fig. 10d. Due to the random tuples distribution on join-matrix models, the execution time of Square and Dynamic is immune to data skewness. Furthermore, our A-DSP uses a hybrid routing strategy which also can be benefited from the random distribution manner.
is similar with ds and tuples per second to is unaffected by uses its own set-
under ¼ and ¼ are 13, 16, 64, 12 and 6, we keep on varying stream vol-
can route join requests more selectively E take minimizing memory usage as the optimization
B ds is ReadJ ¼j
Bi
model can lose advantages of selection operation on group-
Bi
¼1 and we do selectivity,
every three minutes. Accordingly,
Bi
and to denote the
ds. It is always consume the most tasks. This is because/C1
3
Bi
incur less migration cost because
is that
Bi
has only one subgroup for each stream
¼
consume the least tasks, for they
are lacking of CPU resources. While executing
which result from data broadcasting among groups and
is obviously higher than those of bipartite-graph-based ones
of each algorithm. Throughput of matrix-based algorithms
queries.
Fig. 11. Throughput and tuple account of window-based join for different
queries.

In Fig. 10, the execution time of Dynamic is similar with our methods, but it is at the expense of more tasks. Since Bi and Bi6 take minimizing memory usage as the optimization goal, it may decrease processing efficiency when it is lack of CPU resources as shown in Fig. 10d. From Fig. 10 we can conclude that our algorithms are more scalable and efficient.

5.3 Window-based Stream Joins
For this group of experiments, we have 64GB data with window size 180 seconds and slide size 60 seconds. We set stream flow-in rate at about 3 · 10^6 tuples per second to make full use of CPU resources. To facilitate the description, we define the tuple that is distributed to the storage side for join as join request. To further validate the effects of different band-joins and data skewness on system performance, we run window-based joins to testify throughput under different models.

Fig. 11 shows system throughput and average number of join requests received by task in different processing schemes for queries EQ, BNCI and BMRI under different data skewness. Figs. 11a, 11c, and 11e compare throughput of each algorithm. Throughput of matrix-based algorithms is obviously higher than those of bipartite-graph-based ones which result from data broadcasting among groups and are lacking of CPU resources. While executing EQ, under low-skew data, Bi6 can route join requests more selectively to subgroups, guaranteeing the execution efficiency within each task. With severer skewness, however, the amount of data broadcasting among subgroups lows down system performance greatly. While executing BNCI and BMRI, the band-join operations incur more broadcasts among subgroups and aggravate the CPU loads compared to EQ. It is obvious in Fig. 11f, where the large range band-join requests make Bi6 lose advantages of selection operation on grouping data. Because Bi has only one subgroup for each stream and it broadcasts the same amount of data for these three kinds of queries as shown in Figs. 11b, 11d, and 11f. Furthermore, the reason that Bi6 is unaffected by BMRI is that BMRI is a big range band-join. Matrix-based algorithms share the CPU load equally among tasks, but suffer from consuming more tasks. In this group of experiments, the task usages of A-DSP, Square, Dynamic, Bi6 and Bi are 13, 16, 64, 12 and 6, respectively.

5.4 Adaptivity
In order to validate the adaptivity of our processing scheme, we simulate two scenarios as follows: 1) we do selectivity transmission for join operation by altering the calculation range of join predicate; 2) we keep on varying stream volume ratio by v = d2 under the specified total stream volume of 40 GB. Both those experiments are run based on window and all settings are similar to Section 5.3. For the threshold controlling scales out or down, Dynamic uses its own setting in [11] and other algorithms change scheme when memory load is higher than eighty or lower than fifty percent of configured for each task.

5.4.1 Adaptivity on Selectivity Transmission
To better understand our A-DSP can adaptively change the dimensions of its processing architecture to satisfy various operation requirements, we disrupt the time series of Social data and run the Social data query with various selectivity. The different selectivity scenarios are generated by changing the correlative days, i.e., ds, where ds = |S1.date − S2.date|. Specifically, we use ds = 0, ds = 3 and ds = ∞ to denote the equivalent, range and full join operation, respectively. Fig. 12a shows the task consumption of different approaches under above settings. Regardless of the join types, Square and Dynamic always consume the most tasks. This is because they are both based on the fixed matrix architecture. Conversely, both Bi and ReadJ consume the least tasks, for they do not need to store copies of the incoming stream. However, their complicated routing strategies and broadcast action inevitably be an obstacle to the throughput performance, as shown in Fig. 12b. Fig. 12a shows that our A-DSP model can consume resource on-demand, which based on the specific join operation. Furthermore, Fig. 12b reflects A-DSP can enable the system to provide stable high throughput although it consumes less tasks.

5.4.2 Adaptivity on Relative Stream Volume Change
In Fig. 13a, we adjust v every three minutes. Accordingly, the migration volumes of each approach are displayed in Fig. 13b. Both Bi and Bi6 incur less migration cost because they contain the lesser redundant data. However, this is at
the cost of a higher CPU consumption, which inevitably decreases the throughput. Dynamic suffers from high migration cost because this model requires its task number must be a power of two. Our A-DSP algorithm explores the most appropriate processing scheme which takes relatively small migration cost.

5.5 Throughput and Latency

Our synthetic workload generator creates snapshots of tuples for discrete time intervals from an integer key domain $K$. The tuples follow Zipf distributions controlled by skewness parameter $z$, by using the popular generation tool available in Apache project. We use parameter $f$ to control the rate of distribution fluctuation across time intervals. At the beginning of a new interval, our generator keeps swapping frequencies between keys from different task instances until the change on workload is significant enough. i.e., \( L_i(d) > f \). In the above expression, \( L_i(d) \) and \( L_{i-1}(d) \) mean the total workload of task instance $d$ in the $i$th and $(i-1)$th time interval (window), respectively. \( L_i \) means the average load of all tasks in the $i$th time interval. Then, $f$ can be used to denote the workload rangeability of task $d$ between now and the last time interval.

Fig. 14 shows the throughput and latency with varying distribution change frequency running on $EQ_k$ (Figs. 14a and 14b) and $BM_{MR}$ (Figs. 14c and 14d), respectively. In Fig. 14, we draw the theoretical limit of the performance with the line labeled as Ideal, which processing corresponding query using Square in the condition of adequate resources are available. Obviously, Ideal always generates a better throughput and lower processing latency than any others, but cannot be used in real-world application, for its resource waste. When varying the distribution change frequency $f$, both the throughput and latency of $Bi_k$ change dramatically in Figs. 14a and 14b. In particular, $Bi_k$ works well only in the case with less distribution variance (smaller $f$) in Figs. 14a and 14b. In the meantime, both $Bi$ and Dynamic alway have a low throughput and high processing latency in Fig. 14, this is because the broadcast action in $Bi$ and the limit number of task using in Dynamic. On the other hand, our A-DSP algorithm always performs well, with performance very close to the optimal bound set by Ideal.

To expose the cost of our approach in finding the right processing scheme, Fig. 15 shows the adjustment times and migration latency of each approach under varying distribution change frequency. We run this group experiments on $BM_{MR}$ and the relative stream volume change parameter is configured as Fig. 13a. Fig. 15a shows A-DSP incurs more scheme adjustment during the data distribution change. However, its migration latency is still acceptable to the system as shown in Fig. 15b. This is because we have designed a lightweight computation model (Algorithm 4 and Algorithm 5) to support rapid migration plan generation, which incurs minimal data transmission overhead and processing latency. Square uses the same migration plan generation strategies, and it has a similar performance. Dynamic incurs a smaller adjustment time since it adjusts its processing scheme only after the relative stream volume changed. Due to the face that Dynamic needs to maintain a large amount of copy data, its migration latency is the one biggest as shown in Fig. 15b. $Bi$ and $Bi_k$ using the fewest processing tasks make them generate a smaller migration volume and latency.

Fig. 12. Performance under various selectivity.

Fig. 13. Performance with relative stream volume change.

Fig. 14. Throughput and latency with varying distribution change frequency, where (a) and (b) Run on an $EQ_k$, and (c) and (d) on $BM_{MR}$.

Fig. 15. Adjustment times and migration latency with varying distribution change frequency.
always produce a higher
only be one-third of
when the limitation
/C1
costs the most bandwidth. Fig. 17d
as shown in Fig. 17a, its bandwidth usage
have little change in the performance of throughput,
Dynamic
and
on
Weibo datasets with the settings
scales out in
and
10
Bi
Bi
u
r
2-DSP
In recent years, join-matrix model for parallel and
W
A-DSP
Photon [25] is designed by Google to join data
with different available tasks,
can deal with the band-join more
use less tasks for it is mainly designed for memory
S
Bi
Dynamic
and
uses less
¼
Dynamic
RC
is content-insensitive, it pro-
dataset contin-
and
A-DSP
as a matrix, where each
data
by time duration, as computed by
graph.
incoming tuples to all tasks in the other side of bipartite-
is more than ours for it broadcasts the same amount of
tasks than
Stamos et al. [33]
join between two data sets
distributed joins has been restudied. Intuitively, it models a
dynamic data stream in a blocking way on Spark. Though
it upholds θ-join well, under the constraint of window size,
some tuples may miss each other and such batch-mode computing
can only give approximate results. TimeStream [27]
equipped with resilient substitution and dependency tracking mechanisms provides both MapReduce-like batch processing and non-blocking stream processing. However, it suffers from the excessive communication cost due to maintenance of distributed join state. Join-Biclique [12] based on bipartite-graph model supports full-history and window-based stream joins. Compare to the join-matrix model used in DYNAMIC [11], it reduces data backup redundancy and improves resource utilization. In the meantime, considerable efforts have been put on the elasticity feature of the distributed stream processing systems [28], [29], [30], [31], [32], dealing with when and how to efficiently scale in or out computing resources.

6 RELATED WORK
In the early 21st century, considerable researches have been unfolded on designing efficient stream join operators in a distributed environment with a cluster of machines. As mentioned in Section 1, there are two categories model for join operation in distributed stream processing systems, namely 1-DSP and 2-DSP.

1-DSP. Photon [25] is designed by Google to join data streams such as web search queries and user clicks on advertisements. It utilizes a central coordinator to implement fault-tolerant and scalable joining through key-value matching, but cannot handle θ-join. D-Streams [26] adopts mini-batch on continuous data streams in a blocking way on Spark. Though it upholds θ-join well, under the constraint of window size, some tuples may miss each other and such batch-mode computing can only give approximate results. TimeStream [27] equipped with resilient substitution and dependency tracking mechanisms provides both MapReduce-like batch processing and non-blocking stream processing. However, it suffers from the excessive communication cost due to maintenance of distributed join state. Join-Biclique [12] based on bipartite-graph model supports full-history and window-based stream joins. Compare to the join-matrix model used in DYNAMIC [11], it reduces data backup redundancy and improves resource utilization. In the meantime, considerable efforts have been put on the elasticity feature of the distributed stream processing systems [28], [29], [30], [31], [32], dealing with when and how to efficiently scale in or out computing resources.

2-DSP. In recent years, join-matrix model for parallel and distributed joins has been restudied. Intuitively, it models a join between two data sets \( R \) and \( S \) as a matrix, where each side of which corresponds to one relation. Stamos et al. [33] proposed a symmetric fragment and replicate method to support parallel \( \theta \)-joins. This method relies on replicating input tuples to ensure result completeness and extending the fragment and replicate algorithm [34], which suffers from high communication and computation cost. Okcan [13] proposed techniques in MapReduce that adopts join-matrix model and
supports parallel $\theta$-joins. He designed two partitioning scheme, that is 1-Bucket and M-Bucket. 1-Bucket scheme is content-insensitive but incurs high data replication; M-Bucket scheme is content-sensitive in that it maps a tuple to a region based on the join key. Because of the inherent nature of MapReduce, these two algorithms are offline and require that all the data statistics must be available beforehand, which are not suitable for stream join processing. In data stream processing, Elseidy et al. [11] presented a $(n,m)$-mapping scheme partitioning the matrix into $J = n \times m$ equal regions and propose algorithms which adjust the scheme adaptively to data characteristics in real time. However, [11] assumes that the number of partitions $J$ must be powers of two. What’s more, the matrix structure suffers from bad flexibility because when the matrix needs to scale out(down), it must add(remove) the entire row or column cells.

Due to the characteristics of data streams, e.g., infiniteness and instantaneous, conventional join algorithms using blocking operations, e.g., sorting, cannot work any more. For stream join processing, much effort has been put into designing non-blocking algorithms. Wilschutz presents the symmetric hash join SHJ [35]. It is a special type of hash join and assumes that the entire relations can be kept in main memory. For each incoming tuple, SHJ progressively creates two hash tables, one for each relation, and probes them mutually to identify joining tuples. XJoin [36] and DPHJ [37] both extend SHJ by allowing parts of the hash tables to be spilled out to the disk for later processing, greatly enhancing the applicability of the algorithm. Dittrich [38] designed a non-blocking algorithm called PMJ that inherits the advantages of sorting-based algorithms and also supports inequality predicates. The organic combination of XJoin and PMJ is conductive to the realization of HMJ [39], presented by Mokbel. However, all the previous algorithms belong to centralized algorithms and rely on a central entity doing join computation, which cannot be applied in distributed computing directly.

### 7 Conclusion

This paper presents a new parallel stream join mechanism for $\theta$-join in distributed stream processing engines. Inspired by 1-DPS and 2-DPS model, we propose a A-DSP model to promise processing correctness together with efficient resource usage. A-DSP can handle parallel stream joins in a more flexible and adaptive manner, especially to address the demands on operational cost minimization over the cloud platform. Additionally, we design algorithms with moderate complexity to generate task mapping schemes and migration plans to fulfill the objective on operational cost reduction. Empirical studies show that our proposal incurs the smallest cost when the stream join operator is run under the pay-as-you-go scheme. In the future, we will explore the possibility on more flexible and scalable mapping and migration strategies with sampled matrix in pursuit of a smaller migration cost. We will also try to design a new mechanism, to ensure the correctness of processing results when there exist(s) extremely dynamic key(s).

### Acknowledgments

Rong Zhang and Aoying Zhou are supported by the Key Program of National Natural Science Foundation of China (No. 2018YFB1003402) and NSFC (No. 61672233). Kai Zheng is supported by NSFC (No. 61972069, 61836007, 61832017, 61532018). Junhua Fang is supported by NSFC (No.61802273), the Postdoctoral Science Foundation of China under Grant (No. 2017M621813), the Postdoctoral Science Foundation of Jiangsu Province of China under Grant (No. 2018K029C), and the Natural Science Foundation for Colleges and Universities in Jiangsu Province of China under Grant (No. 18KJB520044). Xiaofang Zhou is supported by NSFC (No.61772356). This work is also partially supported by the Major Program of Natural Science Foundation, Educational Commission of Jiangsu Province (No.19KJA610002).

### References

Junhua Fang received the PhD degree in computer science from East China Normal University, Shanghai, in 2017. He is a lecturer in the Advanced Data Analytics Group at the School of Computer Science and Technology, Soochow University, Suzhou. He is a member of CCF. His research interests include distributed database and parallel streaming analytics.

Rong Zhang received the PhD degree in computer science from Fudan University, Shanghai, China, in 2007. She is a member of the China Computer Federation. She joined East China Normal University in 2011 and is currently a professor. From 2017 to 2020, she was an expert researcher at NICT, Japan. Her current research interests include knowledge management, distributed data management, and database benchmarking.

Yan Zhao received the master’s degree in geographic information systems from the University of Chinese Academy of Sciences, Beijing, China, in 2015. She is currently working toward the PhD degree at Soochow University, Suzhou, China. Her research interests include spatial database and trajectory computing.

Kai Zheng received the PhD degree in computer science from the University of Queensland, Brisbane, Australia, in 2012. He is a professor of computer science with the University of Electronic Science and Technology of China, China. He has been working in the area of spatial-temporal databases, uncertain databases, social-media analysis, in memory computing, and block chain technologies. He has published more than 100 papers in prestigious journals and conferences in data management field such as SIGMOD, ICDE, the VLDB Journal, ACM Transactions, and IEEE Transactions. He is a member of the IEEE.

Xiaofang Zhou received the BSc and MSc degrees in computer science from Nanjing University, China, in 1984 and 1987, respectively, and the PhD degree in computer science from the University of Queensland, Australia, in 1994. He is a professor of computer science with the University of Queensland and adjunct professor in the School of Computer Science and Technology, Soochow University, China. His research interests include spatial and multimedia databases, high performance query processing, web information systems, data mining, bioinformatics, and e-research. He is a fellow of the IEEE.

Aoying Zhou is a professor of computer science at East China Normal University (ECNU), where he is heading the School of Data Science & Engineering. Before joining ECNU in 2008, he worked for Fudan University in the Computer Science Department for 15 years. He is the winner of the National Science Fund for Distinguished Young Scholars supported by NSFC and the professorship appointment under the Changjiang Scholars Program of Ministry of Education. He is now acting as a vice-director of ACM SIGMOD China and the Database Technology Committee of China Computer Federation. He is serving as a member of the editorial boards of the VLDB Journal, WWW Journal, and etc. His research interests include data management, in-memory cluster computing, big data benchmarking, and performance optimization.

For more information on this or any other computing topic, please visit our Digital Library at www.computer.org/csdl.